

## Handling Categorical Predictors: plyr, ANOVA, and more

### Group Properties: Kelp

- ▶ Kelp sampled at multiple sites annually
- ▶ At each transect, holdfast diameter and # of fronds counted



How can we get quick summaries by site?, year, or both?

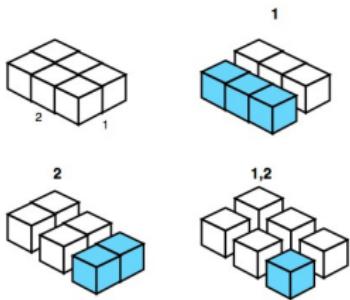
```
#   YEAR MONTH      DATE SITE TRANSECT QUAD SIDE FRONDS
# 2  2000    9 2000-09-28 BULL      1  20       4
# 8  2000    9 2000-09-28 BULL      2  20      11
# 9  2000    9 2000-09-28 BULL      2  20      16
# 10 2000    9 2000-09-28 BULL      2  20      34
# 16 2000    9 2000-09-28 BULL      3  20      27
# 17 2000    9 2000-09-28 BULL      3  20      38
#
#   HL_DIA
# 2      7
# 8     65
# 9     55
# 10    55
# 16    65
# 17    60
```

For loops for Summarization by Site

```
# number of groups
k <- length(levels(kelp$SITE))
#blank means vector
means <- rep(NA, k)
#the loop
for(i in 1:k) {
  #split the data first
  subdata <- subset(kelp, kelp$SITE == levels(kelp$SITE)[i])

  #apply the means function,
  #combine with previous means
  means[i] <- mean(subdata$FRONDS, na.rm=T)
}
```

## The Split, Apply, Combine Strategy



Wickham 2011

## ddply from Hadley Wickham's plyr library

## ddply from Hadley Wickham's plyr library

```

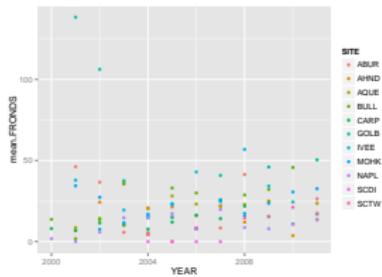
kelpMeans

#      SITE mean.FRONDS
# 1 ABUR      29.26
# 2 AHND      17.63
# 3 AQUE      21.04
# 4 BULL      27.30
# 5 CARP      13.11
# 6 GOLB      42.16
# 7 IVEE      25.81
# 8 MOHK      20.04
# 9 NAPL      13.16
# 10 SCDI      0.00
# 11 SCTW     14.73

```

## Multiple Groups & ddply

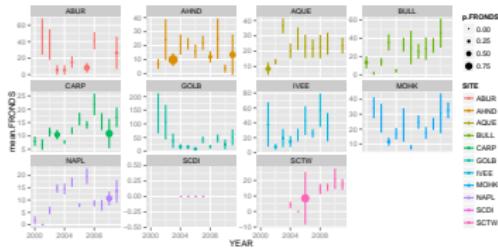
## Multiple Groups & ddply



## Complex Functions & ddply

```
kelpMeans3 <- ddply(kelp, .(YEAR, SITE), function(aFrame){  
  #calculate metrics for a 1-sample T test comparison against  
  #grand mean of 10 fronds/m^2  
  m <- mean(aFrame$FRONDS, na.rm=T)  
  n<-length(na.omit(aFrame$FRONDS))  
  se <- sd(aFrame$FRONDS, na.rm=T)/sqrt(n)  
  t <- (m-10)/se  
  p <- 2*pt(abs(t), df=n-1, lower.tail=F)  
  
  # return everything  
  return(c(mean.FRONDS=m, n.FRONDS=n,  
          se.FRONDS=se, t.FRONDS=t,  
          p.FRONDS = p))  
})
```

## Complex Functions & ddply



## Exercise: Correlation!

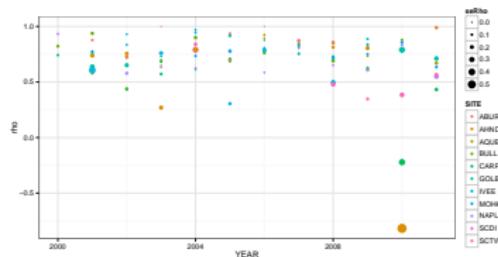
- ▶ Evaluate the correlation between fronds and holdfasts by site and year
- ▶ Plot it
- ▶ Extra: include the SE of the correlation visually



## Exercise: Correlation!

```
kelpCor <- ddply(kelp, .(YEAR, SITE), function(adf){  
  #first get the correlation  
  cors <- cor(adf$FROND, adf$HLD_DIAM)  
  
  #use this to calculate it's SE  
  seCor <- sqrt((1-cors^2) / (nrow(adf)-2))  
  
  #return both  
  return(c(rho = cors, seRho = seCor))  
})
```

## Exercise: Correlation!



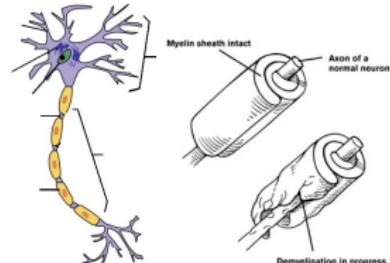
## Many plyr Functions

<i>Input</i>	<i>Output</i>	Array	Data frame	List	Discarded
Array	aaply	adply	alply	a_ply	
Data frame	daply	ddply	dlply	d_ply	
List	laply	ldply	llply	l_ply	

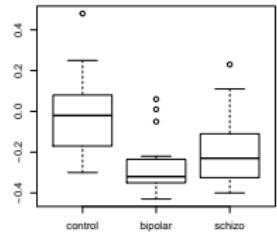
Also r\*ply to replicate an action and return an object. Great for simulation.

See also colwise and each for everyday use!

## Categorical Predictors: Gene Expression and Mental Disorders



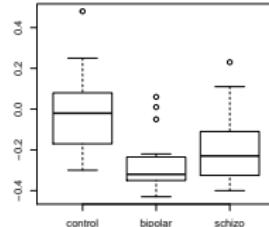
## Categorical Predictors



How do we determine the importance of categorical predictors?

## Aside: Reordering Factors

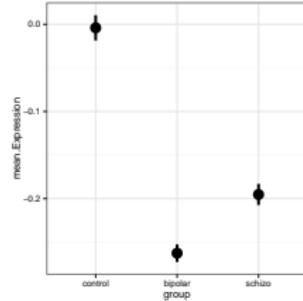
```
brainGene$group <- factor(brainGene$group,  
                           levels=c("control", "bipolar", "schizo"))
```



## Categorical Predictors Ubiquitous

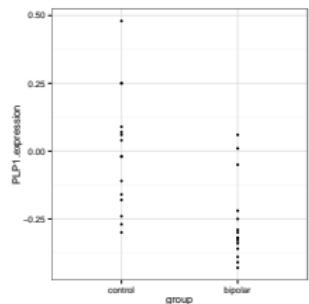
- ▶ Treatments in an Experiment
- ▶ Spatial groups - plots, Sites, States, etc.
- ▶ Individual sampling units
- ▶ Temporal groups - years, seasons, months

## Traditional Way to Think About Categories

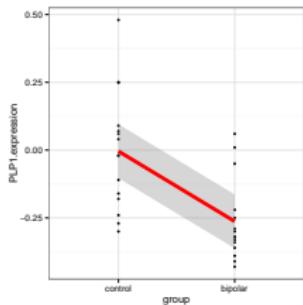


What is the variance between groups v. within groups?

## But How is the Model Fit?

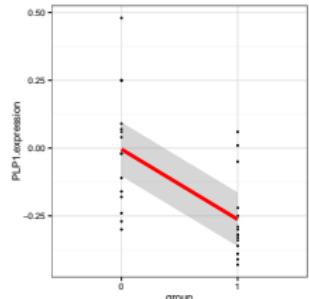


## But How is the Model Fit?



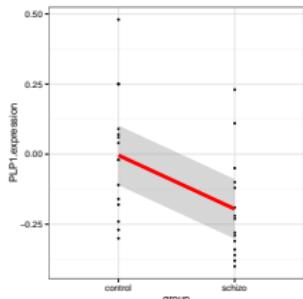
Underlying linear model with control = intercept, dummy variable for bipolar

## But How is the Model Fit?



Underlying linear model with control = intercept, dummy variable for bipolar

## But How is the Model Fit?



Underlying linear model with control = intercept, dummy variable for schizo

## Different Ways to Write a Categorical Model

$$y_{ij} = \bar{y} + (\bar{y}_i - \bar{y}) + (y_{ij} - \bar{y}_i)$$

$$y_{ij} = \mu + \alpha_i + \epsilon_{ij}, \quad \epsilon_{ij} \sim N(0, \sigma^2)$$

$$y_j = \beta_0 + \sum \beta_i x_i + \epsilon_j, \quad x_i = 0, 1$$

$x_i$  indicates presence/absence of a category

Traditional ANOVA special case where all  $x_i$  are orthogonal

Often one category set to  $\beta_0$  for ease of fitting

## This is a Linear Model

```
bg.sub.lm <- lm(PLP1.expression ~ group, data=brainGene)
```

## Hypothesis Testing with a Categorical Model: ANOVA

$$H_0 = \mu_1 = \mu_2 = \mu_3 = \dots$$

OR

$$\beta_0 = \mu, \quad \beta_i = 0$$

## Assumptions of Ordinary Least Squares Regression

- ▶ Independence of data points
- ▶ Normality within groups
- ▶ Homoscedasticity (homogeneity of variance)

## F-Test to Compare

$$SS_{Total} = SS_{Between} + SS_{Within}$$

$$SS_{Between} = \sum_i \sum_j (\bar{Y}_i - \bar{Y})^2, \text{ df=k-1}$$

$$SS_{Within} = \sum_i \sum_j (Y_{ij} - \bar{Y}_i)^2, \text{ df=n-k}$$

To compare them, we need to correct for different DF. This is the Mean Square.

$$MS = SS/DF, \text{ e.g., } MS_W = \frac{SS_W}{n-k}$$

## F-Test to Compare

$$F = \frac{MS_B}{MS_W} \text{ with DF=k-1,n-k}$$

(note similarities to  $SS_R$  and  $SS_E$  notation of regression)

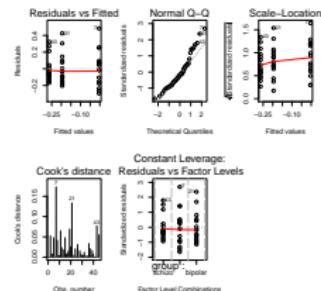
## ANOVA

```
anova(bg.sub.lm)

# Analysis of Variance Table
#
# Response: PLP1.expression
#           Df Sum Sq Mean Sq F value Pr(>F)
# group      2   0.54   0.2701    7.82 0.0013
# Residuals 42   1.45   0.0345
```

## Inspecting Assumptions

```
par(mfrow=c(2,3))
plot(bg.sub.lm, which=1:5 )
```



## Levene's Test of Homogeneity of Variance

```
library(car)

# Loading required package: MASS
# Loading required package: nnet

leveneTest(PLP1.expression ~ group, data=brainGene)

# Levene's Test for Homogeneity of Variance (center = median)
#          Df F value Pr(>F)
# group  2     1.01   0.37
#          42
```

Levene's test robust to departures from normality

## What do I do if I Violate Assumptions?

- ▶ Nonparametric Kruskal-Wallace (uses ranks)
- ▶ Transform?
- ▶ GLM with ANODEV

## Kruskal Wallace Test

```
kruskal.test(PLP1.expression ~ group, data=brainGene)

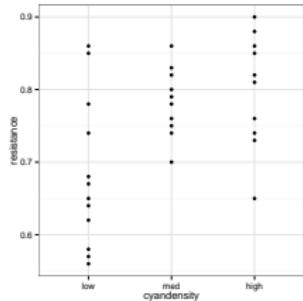
#
# Kruskal-Wallis rank sum test
#
# data: PLP1.expression by group
# Kruskal-Wallis chi-squared = 13.2, df = 2, p-value =
# 0.001361
```

## Exercise: Daphnia Resistance

- ▶ Plot the mean and SE of the data by group
- ▶ Evaluate whether the data is appropriate for ANOVA
- ▶ Fit an ANOVA and check diagnostics
- ▶ Evaluate results & compare to Kruskal-Wallace and a glm with a Gamma distribution



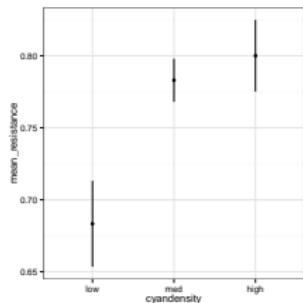
## Daphnia Data



## Daphnia Means

```
#first use plyr to get means and SE
dsummary <- ddply(daphnia, .(cyandensity), summarize,
                  mean_resistance = mean(resistance),
                  se = sd(resistance) / sqrt(length(resistance)))
#
ggplot(dsummary, aes(x=cyandensity, y=mean_resistance,
                      ymin=mean_resistance-se,
                      ymax=mean_resistance+se)) +
  geom_pointrange() + theme_bw()
```

## Daphnia Means



## How about HOV?

```
leveneTest(resistance ~ cyandensity, data=daphnia)

# Levene's Test for Homogeneity of Variance (center = median)
#          Df F value Pr(>F)
# group     2      2   0.15
#          29
```

## ANOVA shows an Effect

```
daphniaLM <- lm(resistance ~ cyandensity, data=daphnia)
anova(daphniaLM)

# Analysis of Variance Table
#
# Response: resistance
#           Df Sum Sq Mean Sq F value Pr(>F)
# cyandensity  2 0.0892  0.0446   6.69 0.0041
# Residuals   29 0.1933  0.0067
```

## KW shows an Effect

```
# Kruskal-Wallis rank sum test
#
# data: resistance by cyandensity
# Kruskal-Wallis chi-squared = 8.2, df = 2, p-value =
# 0.01658
```

## Bad GLM Does Not

```
# Analysis of Deviance Table
#
# Model: Gamma, link: identity
#
# Response: resistance
#
# Terms added sequentially (first to last)
#
#
#          Df Deviance Resid. Df Resid. Dev
# NULL                 31      0.529
# cyandensity  2     0.162      29      0.367
```

## Diagnostics Also Good

